Some Stability and Boundedness Results for the Solutions of Certain Fourth Order Differential Equations

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Abstract

Sufficient conditions are established for the asymptotic stability of the zero solution of the equation (1.1) with $p \equiv 0$ and the boundedness of all solutions of the equation (1.1) with $p \neq 0$. Our result includes and improves several results in the literature ([4], [5], [8]).

Key words: Differential equations of fourth order, boundedness, stability, Lyapunov functions.

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1 Introduction

In the current paper, we consider the nonlinear differential equation of the form

$$x^{(4)} + a(\ddot{x}, \ddot{x}) \, \ddot{x} + b(x, \dot{x}) \, \ddot{x} + c(\dot{x}) + d(x) = p(t, x, \dot{x}, \ddot{x}, \ddot{x}). \tag{1.1}$$

It can be written in the phase variables form

$$\dot{x} = y, \quad \dot{y} = z, \quad \dot{z} = u, \dot{u} = -a(z, u)u - b(x, y)z - c(y) - d(x) + p(t, x, y, z, u),$$
(1.2)